# BHARATHI WOMEN'S COLLEGE (AUTONOMOUS) 

CHENNAI - 600108

## DEPARTMENT OF MATHEMATICS


(SEMESTER WITH CHOICE BASED CREDIT SYSTEM)

UG SYLLABUS

B.Sc. MATHEMATICS

(2019-2020 onwards)



## DEPARTMENT OF MATHEMATICS

## INTERNAL ASSESSMENT PATTERN

## THEORY PAPERS

## INTERNAL MARKS - $\mathbf{2 5}$

TEST : 10

ASSIGNMENT : 10
MODEL EXAM : 25
ATTENDANCE : 5
TOTAL : 50
REDUCED TO : 25

## PRACTICAL

## INTERNAL TOTAL MARKS - 40

RESULT AND ACCURACY : 10
RECORD : 10
TEST : 5
MODEL EXAM : 10
ATTENDANCE : 5
EXTERNAL TOTAL MARKS - 60
SUBMISSION OF RECORD : 10
ANSWER 2 OUT OF 4 QUESTION $2 \times 25: 50$

## ATTENDANCE BREAK UP

Below 50\% 50\% to64\%
65\% to $74 \%$
$75 \%$ to $89 \%$
$90 \%$ to $100 \%$

REDO the semester
Not Eligible for the current semester - 2 marks
3 Marks (Con-donation)
4 Marks
5 Marks

Website for Online Reference : http://nptel.ac.in

# BHARATHI WOMEN'S COLLEGE (AUTONOMOUS), CHENNAI-600 108 DEPARTMENT OF MATHEMATICS 

## PATTERN OF QUESTION PAPER

1. CORE / ALLIED and ELECTIVE SUBJECTS
(QUESTION TO BE SET NOT OMITTING ANY UNIT IN ALL THE SECTIONS)

SECTION A
10 QUESTIONS - NO CHOICE
SECTION B
ANSWER 5 OUT OF 7 QUESTIONS
SECTION C
ANSWER 3 OUT OF 5 QUESTIONS
TOTAL

10 * 2 = 20 MARKS

5 * 5 = 25 MARKS
$3 * 10=30$ MARKS

75 MARKS
2. NME / SBE / VBE
(QUESTION TO BE SET NOT OMITTING ANY UNIT IN ALL THE SECTIONS)
SECTION A
5 * 5 = 25 MARKS
ANSWER 5 OUT OF 7
SECTION B
$5 * \mathbf{1 0}=\mathbf{5 0}$ MARKS
ANSWER 5 OUT OF 8
TOTAL
75 MARKS

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 <br> B.Sc. - MATHEMATICS <br> CORE PAPER I - ALGEBRA AND TRIGONOMETRY 

(For the students admitted from the year 2019-2020)

HOURS/WEEK : 5
CREDITS : 5

SEMESTER : I
SUBJECT CODE: 19CAA

## OBJECTIVE

To develop problem solving and computing skills, and to impart basic knowledge in trigonometry and number theory.

## UNIT I

Summation of series: Binomial, Exponential and Logarithmic series (without proofs) - Simple problems.
Algebra Volume I: Chapter 3- sections 10
Chapter 4-sections 3, 5, 6, 7 and 9.
UNIT II
Symmetric function of the roots in terms of coefficients - Transformations of equations - Roots with signs changed, Roots multiplied by a given number, Reciprocal roots - Reciprocal equations Increasing and diminishing the roots,.
Algebra Volume I: Chapter 6- sections 12 and 15-17.

## UNIT III

Symmetric - Skew symmetric - Hermitian - Skew Hermitian - Orthogonal and Unitary Matrices

- Eigen Values and Eigen Vectors - Similar Matrices - Cayley Hamilton theorem - Diagonalization of a Matrix.
Algebra Volume II: Chapter 2- sections 6, 9, and 16.


## UNIT IV

Prime Number - Composite Number - Decomposition of a Composite Number as a Product of Primes uniquely (without proof) - Divisors of a Positive Integer - The Theory of Congruence - Basic Properties of Congruence - Euler Function (without Proof) - Highest Power of a Prime Number p contained in n ! - Fermat's and Wilson's Theorems (without proof).
Algebra Volume I: Chapter 5- sections 1-13, 16(omit 16.1), 17.

## UNIT V

Expansions of $\cos \mathrm{n} \theta, \sin \mathrm{n} \theta-$ Expansion of $\tan \mathrm{n} \theta$ in terms of $\tan \theta$-. Powers of sines and cosines of $\theta$ in terms of functions of multiples of $\theta$ - Expansions of $\sin \theta$ and $\cos \theta$ in a series of ascending powers of $\theta$ - Hyperbolic Functions - Relation between Hyperbolic Functions and trigonometric functions- Inverse Hyperbolic Functions.
Trigonometry: Chapter 3-sections 1, 2 and 4, Chapter 4- sections 1 and 2.
BOOKS FOR STUDY

1. T.K. Manicavachagom Pillai, T. Natarajan and K.S. Ganapathy,Algebra Volume I and II, S. Viswanathan Publishers Pvt. Ltd., 2008.
2. S. Narayanan and T.K. Manicavachagam Pillai, TrigonometryS. Viswanathan Publishers Pvt.Ltd., 2006.

## BOOKS FOR REFERENCE

1. Arumugam S, Thangapandi Issac, Classical Algebra, New Gamma Publishing House, Palayamkottai.
2. Burnside W.S. and A.W. Panton, Theory of Equations, Dublin University Press, 1954.
3. Kumaravelu S and SusheelaKumaravelu, Elements of Number Theory, Nagarcoil, 2002.
4. Arumugam S, Thangapandi Issac A, Trigonometry,New Gamma Publishing House, 2017.

## OUTCOME OF LEARNING

Students will be able to

- Find the sum of the series: Binomial, Exponential and Logarithmic.
- Compute the Eigen values and Eigen vectors and inverse of a matrix using Cayley Hamilton Theorem.
- Understand the results on prime number and also to find the Sum, product of all the divisiors of N .
- Expand $\cos n \theta, \operatorname{sinn} \theta$ and $\operatorname{tann} \theta$ in terms of $\theta$ and define hyperbolic and inverse hyperbolic functions.


## BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER II - DIFFERENTIAL CALCULUS <br> (For the students admitted from the year 2019-2020)

CREDITS : 4 SUBJECT CODE: 19CAB

## OBJECTIVE

To impart an exhaustive knowledge in partial differentiation and to explain the use of differential calculus to solve physics, geometry and optimization problems.

## UNIT I

Partial differentiation - Function of function rule - Total Differential co-efficient -Implicit function - Homogeneous function - Partial derivatives of a function of two functions - Jacobians Simple problems.
Chapter 8: Section 1.1 - 1.7 \& Volume II Chapter 6: Section 1.1 (Book-1)
Chapter 2: Section 10 (Book-2)

## UNIT II

Maxima and minima of functions of 2 and 3 independent variables - Necessary and sufficient conditions (without proof) - Lagrange's method (without Proof) - Simple problems on these concepts.

Chapter 8: Section 4, 5 (Pg. No. 222 - 240) (Book-1)

## UNIT III

Curvature - Radius of curvature in Cartesian and Polar co-ordinates - p-r equations- Centre of Curvature.
Chapter 10: Section 2.1 - 2.4, 2.6, 2.7. (Book-1)
UNIT IV
Evolutes - Envelopes - Method of finding envelopes (one parameter and two parameter family). Chapter 10: Section 2.5, 1.1-1.4. (Book-1)

## UNIT V

Asymptotes - Asymptotes of plane algebraic curves - Asymptotes parallel to the axis - Special cases- Another method of finding asymptotes- Asymptotes by inspection.

## Chapter 11: Section 1 - 6. (Book-1)

## BOOKS FOR STUDY

1. S. Narayanan, and T.K. Manicavachagom Pillai, Calculus Volume - I, S. Viswanathan Publishers.
2. P. Kandhasamy and K. Thilagavathy, Mathematics Volume - I, S.Chand \& Company, 2004.

## BOOKS FOR REFERENCE

1. P. R. Vittal, Differential Calculus, Margam Publishers.
2. Shanthi Narayanan,P.K.Mittal, Differential Calculus, S.Chand Publishing.

## OUTCOME OF LEARNING

Students understood the concepts of implicit function, homogeneous function, partial derivatives of a function of two functions, Jacobians, Lagrange's method, Maxima and minima, Curvature, Evolutes, Envelopes and Asymptotes.

## BHARATHI WOMEN'S COLLEGE(AUTONOMOUS), CHENNAI-600 108 B.Sc. - MATHEMATICS ALLIED PAPER I - NUMERICAL METHODS - I

(For the students admitted from the year 2019-2020)

## HOURS/WEEK : 6

CREDITS : 5

SEMESTER : I<br>SUBJECT CODE: 19AAA

## OBJECTIVE

To learn the iterative methods of finding the roots of algebraic and transcendental equations and also to find the eigen values and eigen vectors of matrices. To acquire knowledge in solving the system of linear algebraic equations by direct and indirect methods. To introduce the operators in finite differences and to understand the numerical techniques of interpolation in equal and unequal intervals.

## UNIT I

Solution of numerical algebraic and transcendental equations - Bisection method, Iteration method, Regula falsi method, Newton-Raphson method.

## Chapter 3: Sections 3.1-3.4

## UNIT II

Solution of simultaneous linear algebraic equations - Gauss-Elimination method, Gauss-Jordan method, Gauss-Jacobi method, Gauss-Seidal method - Eigen values of a matrix by power method.

## Chapter 4: Sections 4.1-4.2, 4.8-4.9 and 13.1

## UNIT III

Finite Differences $-\Delta, \nabla$, E operators and relation between them, Differences of a polynomial, Factorial polynomial, differences of zero, summation of series.
Chapter 5: Sections 5.1-5.5 and 5.7

## UNIT IV

Interpolation with equal intervals - Newton's Forward and Backward interpolation formula, Central differences formula, Gauss forward and backward formula, Stirling's formula and Bessel's formula.
Chapter 6: Sections 6.1-6.7, 7.1-7.6.

## UNIT V

Interpolation with unequal intervals - Divided differences and Newton's divided difference formula for interpolation and Lagrange's formula for interpolation - Inverse interpolation - Lagrange's method.
Chapter 8: Sections 8.1-8.8

## BOOKS FOR STUDY

P. Kandasamy, K. Thilagavathy and K. Gunavathy,Numerical Methods,2003, S.Chand \&Co.

## BOOKS FOR REFERENCE

1. Gupta Malik, Calculus Of Finite Differences And Numerical Analysis, Krishna Prakasan Mandir, Meerut
2. M.K. Venkataraman, Numerical Methods in Science and Engineering, National publishing house, Chennai.
3. B.D.Gupta, Numerical Analysis, KonarkE publishing.
4. Saxena, Calculus of Finite Differences and Numerical Analysis, S. Chand \& Co.

## OUTCOME OF LEARNING

Students will be able to

- Obtain numerical solutions of algebraic and transcendental equations.
- Find numerical solutions of system of linear equations and check the accuracy of the solutions.
- Acquire knowledge on various operators and factorial polynomial.
- Determine the eigen values of a matrix by power method.
- Understand the various interpolating methods for equal and unequal intervals.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 

 B.Sc. - MATHEMATICSALLIED I PAPER I -ALLIED MATHEMATICS - I
(For Physics, Chemistry \& Computer Science courses)
(For the students admitted from the year 2019-2020)

| HOURS/WEEK : 6 | SEMESTER : I |
| :--- | ---: | :--- |
| CREDITS $: 5$ | SUBJECT CODE: 19AAP |

## OBJECTIVE

To introduce the basic concepts of Algebra, Trigonometry and Calculus.To develop mathematical skills for solving the problems in other branches of science.

## UNIT I

Algebra and Trigonometry: Solution of third degree equations whose roots are in A.P, G.P and H.P - Reciprocal equations - Expansion of $\sin n \theta, \cos n \theta$ in terms of $\sin \theta$ and $\cos \theta$ - Expansion for $\cos ^{\mathrm{n}} \theta, \sin ^{\mathrm{n}} \theta$ in terms of multiple angles of $\theta$.
Algebra- Chapter 1:Page No. 39-47, Chapter-2 Page No. 56-63
Trignometry- Chapter 1:Page No. 196-210

## UNIT II

Differential Calculus: Jacobian - Curvature and radius of curvature in Cartesian Coordinates and polar coordinates.
Differential Calculus - Chapter 2: Page No. 246-251; Chapter-4 Page No. 261-273

## UNIT III

Integral Calculus: Reduction formula $\left(\int \sin ^{n} x d x, \int \cos ^{n} x d x\right.$ and $\left.\int \sin ^{m} x \cos ^{n} x d x\right)$, Properties of definite integrals (without proof). Multiple Integrals: Evaluation of double \& triple integrals (Cartesian co-ordinates only) - Simple problems.

## Integral Calculus- Chapter2: Page No.: 53-60: Chapter 3: Page No. 61-63

Multiple Integrals -Chapter 4: Page No. 83-87; 91-95

## UNIT IV

Laplace Transforms - Definition - Sufficient condition - Standard functions - Simple problems (excluding periodic function).
Laplace Transforms- Page No.234-248

## UNIT V

Inverse Laplace Transforms - Applying Laplace Transforms to find solution of second order linear differential equations (constant coefficients) - Simple problems.
Laplace Transforms- Page No.248-284

## BOOK FOR STUDY

P.Kandasamy \& K.Thilagavathy, Allied Mathematics Volume I \& II, 2003,2004, S.Chand \& Co.

## BOOKS FOR REFERENCE

1. Narayanan \& Manickavachagom Pillai, Allied Mathematics, S. Viswanathan Publishers
2.P.R.Vittal, Allied Mathematics, Margham Publications.
3.P. Duraipandian \& S. Uayabaskaran, Allied Mathematics Volume I \& II.
4.P. Balasubrahmanyam and K.G.Subramanian, Ancillary MathematicsVolume I \& II, Tata McGraw Hill Publishing Company Ltd., New Delhi.

## OUTCOME OF LEARNING

Students will be able to

- Solve the equations upto $3^{\text {rd }}$ degree and also to solve the reciprocal equations.
- Expand $\cos n \theta, \operatorname{sinn} \theta$ and $\operatorname{tann} \theta$ in terms of $\theta$ and define hyperbolic and inverse hyperbolic functions.
- Determine Jacobians, Curvature and radius of curvature.
- Solve basic integral calculus problems and multiple integrals.
- Apply the basic properties of Laplace transform and to solve the linear differential equations by using Laplace transform.


## BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER III - INTEGRAL CALCULUS

(For the students admitted from the year 2019-2020)

```
HOURS/WEEK : 5
SEMESTER : II
CREDITS :5 SUBJECT CODE: 19CAC
```


## OBJECTIVE

To introduce the fundamental principles, concepts and knowledge in the area of integral calculus. To prepare the students for applying these concepts to other courses.

## UNIT I

Integrals of the type $\int \frac{d x}{a+b \cos x}, \int \frac{d x}{a+b \sin x}$ and $\int \frac{d x}{a^{2} \cos ^{2} x+b^{2} \sin ^{2} x}$ Properties of definite integrals - Integration by parts- Simple problems.

Chapter 1: Sections 9-12

## UNIT II

Reduction formula - Integrals of the type $\int e^{a x} \cos b x d x$ and $\int e^{a x} \sin b x d x$ - Bernoulli's formula -Simple problems.

## Chapter 1: Sections 13-15.1

## UNIT III

Double integrals (both Cartesian and Polar co-ordinates) - Change of order of integration.
Chapter 5: Sections 1 - 3

## UNIT IV

Triple integrals - Applications of multiple integrals.

## Chapter 5: Sections 4-5

## UNIT V

Beta and Gamma functions - Properties and simple problems, Application of Beta and Gamma functions in evaluation of double integrals.

Chapter 7: Sections 1 - 6

## BOOK FOR STUDY

S. Narayanan and T.K Manicavachagom Pillai, Calculus Volume II, S. Viswanathan (Printers \& Publishers) Pvt. Ltd.,

## BOOKS FOR REFERENCE

1. Kandasamy P and Thilagavathi K., Mathematics for B.Sc Volume II, S.Chand\& Company Ltd., NewDelhi-55.
2. Arumugam S and Thangapandi Issac A, Calculus, New Gamma Publishing House.

## OUTCOME OF LEARNING

Students will able to

- Solve basic integral calculus problems, explain properties of definite integrals, prove reduction formulae and solve some problems by using these formulae.
- Evaluate double and triple integrals and also evaluating by changing the order of integration.
- Apply basic properties of beta and gamma functions for the evaluation of integrals.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER IV - DIFFERENTIAL EQUATIONS \& LAPLACE TRANSFORMS 

(For the students admitted from the year 2019-2020)

| HOURS/WEEK : 4 | SEMESTER : II |
| :--- | :--- | :--- |
| CREDITS $: 4$ | SUBJECT CODE: 19CAD |

HOURS/WEEK : 4
SUBJECT CODE: 19CAD

## OBJECTIVE

To apply the appropriate analytic techniques for finding the solutions of ordinary differential equations. To equip students with the concepts of forming and solving partial differential equations.To inculcate the importance of one of the integral transforms- Laplace transforms which has many applications in physics and engineering.

## UNIT I

First order but of higher degree equations solvable for $p$, solvable for $x$, solvable for $y-$ Clairaut's form - Simple problems.
Chapter 1: Section 5.1-5.5, 6.1

## UNIT II

Second order equations with constant co-efficients with particular integrale $e^{a x} \sin n x, e^{a x} \cos n x$, $e^{a x} x^{n}$ - Second order differential equations with variable coefficients.

## Chapter 2: Section 4, 8

## UNIT III

Formation of P.D.E by eliminating arbitrary constants and arbitrary functions - Complete integral -Singular integral - General integral - Standard types $\mathrm{f}(\mathrm{p}, \mathrm{q})=0, \mathrm{f}(x, p, q)=0, \mathrm{f}(y, p, q)=0, \mathrm{f}(z, p, q)$ $=0, \mathrm{f}_{1}(x, p)=\mathrm{f}_{2}(y, q)$ - Clairaut's form and Lagrange's equation $\mathrm{P} p+\mathrm{Q} q=\mathrm{R}$ - Simple problems.
Chapter 4: Sections 1-6.

## UNIT IV

Laplace Transforms - Definition - sufficient condition - standard functions - Initial and final value theorem - simple problems (excluding periodic function).
Chapter- 5: Sections 1-5.

## UNIT V

Inverse Laplace Transforms (Usual type) - Convolution theorem (without proof) - Applying Laplace Transforms to find solution of first and second order linear differential equations (constant coefficients) - simple problems.
Chapter- 5: Sections 6 - 10.

## BOOK FOR STUDY

S. Narayanan and T.K. Manickavachagam Pillai, Calculus Volume III, S.Viswanathan Pvt. Ltd.

## BOOK FOR REFERENCE

S.Sankarappan and S.Kalavathy,Differential Equations \& Laplace Transforms, Vijay Nicole Imprints Pvt. Ltd.

## OUTCOME OF LEARNING

Students will be able to

- Find solution of higher-order linear differential equations with constant and variable coefficients.
- Formulate partial differential equations by eliminating arbitrary constants and functions.
- Apply the basic properties of Laplace transform and inverse Laplace transform to solve the linear differential equations.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> ALLIED I PAPER II - NUMERICAL METHODS - II <br> (For the students admitted from the year 2019-2020) 

```
HOURS/WEEK : }
SEMESTER : II
CREDITS :5
SUBJECT CODE: 19AAB
```


## OBJECTIVE

To understand the numerical techniques of differentiation and integration of interpolating polynomials. To learn the methods of solving second order difference equations. To find the numerical solution of first order ordinary differential equations with initial conditions and the partial differential equations with initial and boundary conditions by using different methods.

## UNIT I

Numerical Differentiation and Integration - Derivatives using Newton's forward and backward difference formulae, General quadrature formula, Trapezoidal rule, Simpson's one-third rule, Simpson's three-eighth rule.
Chapter 9: Sections 9.1-9.3, 9.7-9.9, 9.13-9.14

## UNIT II

Difference Equations - Linear homogenous and non-homogeneous difference equation with constant coefficients, particular integrals for $\mathrm{a}^{\mathrm{n}} \mathrm{x}^{\mathrm{m}}, \mathrm{x}^{\mathrm{m}}, \sin \mathrm{kx}, \cos \mathrm{kx}$.
Chapter 10: Sections 10.1-10.7

## UNIT III

Numerical solution of Ordinary Differential Equations - Numerical Solution of ordinary differential equations (first order only) by Taylor's series method, Euler's method, Modified Euler's method.
Chapter 11: Sections 11.5, 11.9, 11.11

## UNIT IV

Numerical solution of Ordinary Differential Equations - Runge-kutta second order and fourth order methods only, Multi step method - Milne's and Adam's predictor and corrector methods.

## Chapter 11: Sections 11.13, 11.17and 11.18

## UNIT V

Numerical solutions of Partial Differential Equations - Difference Quotient, Elliptic equations, Poisson equations, Parabolic equations.
Chapter 12: Sections 12.1-12.9

## BOOK FOR STUDY

P. Kandasamy, K. Thilagavathy \& K. Gunavathy, Numerical Methods, 2003, S.Chand \& Company Ltd.

## BOOKS FOR REFERENCE

1. Gupta Malik, Calculus Of Finite Differences And Numerical Analysis, Krishna Prakasan Mandir, Meerut
2. M.K. Venkataraman, Numerical Methods in Science and Engineering, National publishing house, Chennai.
3. B.D.Gupta, Numerical Analysis, Konark E publishing.
4. Saxena, Calculus of Finite Differences and Numerical Analysis, S. Chand \& Co.

## OUTCOME OF LEARNING

Students will be able to

- Solve initial and boundary value problems in ordinary and partial differential equations and difference equations using numerical methods.
- Apply various numerical methods in real life problems.

```
BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108
                        B.Sc. - MATHEMATICS
    ALLIED I PAPER II - ALLIED MATHEMATICS - II
    (For Physics, Chemistry & Computer Science courses)
    (For the students admitted from the year 2019-2020)
```

HOURS/WEEK : 6
CREDITS : 5

SEMESTER : II
SUBJECT CODE: 19AAQ

## OBJECTIVE

To introduce the basic concepts of Finite differences, Vector calculus and Fourier series in order to develop mathematical skills and solve the problems in other branches of science.

## UNIT I

Finite Differences: Arguments, entry differences, differential tables, Operators $\Delta$, E, , Newton's forward, backward formula, Lagrange's interpolation formula.
Finite Differences:Page No. 147-195.

## UNIT II

Ordinary differential equation: Second order differential equation with constant coefficients Particular integrals for $e^{a x}, x^{m}, \sin m x, \cos m x$.
Differential Equations: Chapter 3:Page No. 42 - 58.

## UNIT III

Vector Calculus: Introduction - Gradient - Divergence - Curl - Solenoidal and Irrotational Vectors - Directional derivative - Unit Normal to a surface.
Vector Analysis: Chapter 2: Page No. 306-320.

## UNIT IV

Gauss, Stokes and Green's theorems (without proof) - Simple problems on square, rectangle, cube and cuboid.
Vector Analysis: Chapter 3: Page No. 321 - 344.

## UNIT V

Fourier Series: Dirichlets' conditions- Fourier series of functions with period $2 \pi$ - Fourier series of odd and even functions.
Fourier Series:Page No. 140 - 159.

## BOOK FOR STUDY

P.Kandasamy \& K.Thilagavathy, Allied Mathematics Volume I \& II, 2003, 2004, S.Chand \& Co.

## BOOKS FOR REFERENCE

1. Narayanan \& Manickavachagom Pillai, Allied Mathematics,S. Viswanathan Publishers 2. P.R.Vittal, Allied Mathematics,Margham Publications.
2. P. Duraipandian \& S. Udayabaskaran, Allied Mathematics Volume I \& II.
4.P. Balasubrahmanyam and K.G.Subramanian, Ancillary MathematicsVolume I \& II, Tata McGraw Hill Publishing Company Ltd., New Delhi.

## OUTCOME OF LEARNING

Students will be able to

- Apply various operators and also to solve various interpolating methods for equal and unequal intervals.
- Find solution of second order linear differential equations with constant coefficients.
- $\quad$ Solve problems using vector differentiation and integration.
- Find the Fourier series for the periodic functions.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER V - ANALYTICAL GEOMETRY 

(For the students admitted from the year 2019-2020)
HOURS/WEEK : 4
SEMESTER : III
CREDITS : 4
SUBJECT CODE: 19CAE

## OBJECTIVE

Students are exposed to fundamental aspects of Two Dimensional Analytical Geometry and it develops logical and systematic computational skills. To give basic ideas of the three dimensional coordinate system and to have a thorough knowledge of Sphere, Cone and Cylinder.

## UNIT I

Polar, Pole, Co-normal, concyclic-Parabola and Ellipse.
Chapter VI: sec. 6, 6.1,11,12
Chapter VII:sec. 7,7.1, 12, 12.1, 13

## UNIT II

Conjugate diameters for Ellipse and Hyperbola. Hyperbola- Asymptotes, Angle between the asymptotes, Properties of Asymptotes.

## Chapter VII: sec. 16, 16.1-16.3

Chapter VIII: sec. 4-9 (excluding 7)

## UNIT III

The Sphere: General equation - Equation of a sphere with given centre and radius - Length of the tangent from the given point to the sphere - Plane section of a sphere - Intersection of two spheres - Tangent plane to a sphere.

Chapter IV - Section: 1 - 8

## UNIT IV

Cone: Necessary condition for a general equation of second degree to represent cone - Right circular cone - Tangent plane - Normal - Angle between the lines in which the plane cuts the cone.

## Chapter V-Section: 1-7

## UNIT V

Cylinder: Equation of the cylinder whose generators are parallel to the line with given guiding curve - Right circular cylinder - Enveloping cylinder.

## Chapter V - Section: 8

## BOOKS FOR STUDY

1. T.K. Manicavachagom Pillay and T.Natarajans, Analytical Geometry Part I 2D, S. Viswanathan Publishers Pvt. Ltd., 2008.
2. T.K. Manicavachagom Pillay and T.Natarajans, Analytical Geometry Part II 3D, S. Viswanathan Publishers Pvt. Ltd., 2012.

## BOOKS FOR REFERENCE

1. Shanti Narayan and Dr. P.K. Mittal,Analytical Solid Geometry, S Chand and Company Ltd., New Delhi.
2. S. Narayanan and T.K.Manicavachagom Pillay, Calculus Volume III, S.Viswanathan Pvt. Ltd.
3. P. Duraipandian and Lakshmi Duraipandian, Analytical Geometry 3D, Emerald Publishers and Distributors.

## OUTCOME OF LEARNING

Students will be able to

- Determine the locus of the pole of tangents, normals and chord under any geometric conditions.
- Formulate various forms of equation of a Sphere, Cone and Cylinder.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER VI - VECTOR CALCULUS AND FOURIER SERIES <br> (For the students admitted from the year 2019-2020) 

## HOURS/WEEK : 4

CREDITS : 4

SEMESTER : III
SUBJECT CODE: 19CAF

## OBJECTIVE

To introduce and develop the methods of vector analysis which are fundamental tool in many theories of Applied Mathematics. To understand the various integral theorems relating line, surface and volume integrals. To understand Fourier series representation of periodic functions.

## UNIT I

Vector differentiation - Gradient - Divergence - Curl-Directional derivative - Unit normal to a surface.
Vector Analysis: Chapter 1, 2, 3

## UNIT II

Vector Integration - Line, surface and volume integrals.
Vector Analysis: Chapter 5

## UNIT III

Theorems of Gauss, Stokes and Green's (without proof) - Simple problems.
Vector Analysis: Chapter 6

## UNIT IV

Dirichlet's condition - Fourier series expansions of periodic function with period $2 \pi$ and $2 l-$ Odd and Even functions.
Fourier Series:Page No. 96-134.

## UNIT V

Half range series (both 0 to $\pi$ and 0 to $l$ ) - Complex form of Fourier series - Parseval's Identity - Harmonic Analysis.

Fourier Series:Page No. 135 - 189.

## BOOKS FOR STUDY

1. P. Duraipandian and Kayalal Pachaiyappa, Vector Analysis, Muhil Publishers.

2 P.Kandaswamy, K.Thilagavathy\& K.Gunavathy, Mathematics Volume IV, S Chand \& Co., 2005.

## BOOKS FOR REFERENCE

1. P.R.Vittal,Vector Calculus, Fourier series and Fourier Transform, Margham Publications, Chennai.
2. M.K.Venkataraman, Engineering Mathematics-Part B, National Publishing Company, Chennai.
3. B.S.Grewal,Higher Engineering Mathematics, Khanna Publishers, New Delhi.

## OUTCOME OF LEARNING

Students will be able to

- Solve problems using vector differentiation and integration.
- Understand that any periodic function can be expressed as Fourier series.
- Expand an odd or even function as a half range cosine or sine Fourier series.
- Obtain the complex exponential Fourier series of a function and also known to find the solution numerically by using Harmonic analysis.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> ALLIED II PAPER I - MATHEMATICAL STATISTICS - I <br> (For the students admitted from the year 2019-2020) 

```
HOURS/WEEK : 6
SEMESTER : III
CREDITS : 5
SUBJECT CODE: 19AAC
```


## OBJECTIVE

To build the basis for promoting theoretical and application aspects of statistics. To emphasis the relevance of statistical tools and techniques of analysis in the study of inter disciplinary sciences.

## UNIT I

Measures of Central Tendency-Measures of Dispersion, Moments, Skewness and Kurtosis

## Chapter-2 Sections 2.3-2.9; <br> Chapter 3 Sections 3.1-3.9(3.9.1 \& 3.9.2), 3.10, 3.11\&3.12

## UNIT II

Probability of an event - Definition (Classical and Empirical) - Axiomatic approach to probability - Addition and Multiplication Laws of probability - Independent events - Conditional probability-Baye's Theorem
Chapter - 4 Sections 4.1-4.8(omit sections 4.6.3 \& 4.7.1)

## UNIT III

Random variables - Distribution function - Discrete and continuous Random variable - Two dimensional random variable- Marginal and conditional distributions and independence of random variables.
Chapter - 5 Sections 5.1-5.5 (omit section 5.6)

## UNIT IV

Mathematical Expectation- Addition \& Multiplication theorem of Expectation- Co-varianceConditional Expectation and conditional Variance -Moment generating function -Definition and properties - Characteristic function-Definition and properties-Uniqueness theorem of Characteristic function - Chebyshev's inequality- Simple Problems.
Chapter - 6 Sections 6.1-6.12 (omit section 6.10)

## UNIT V

Correlation and Regression - Correlation- scatter Diagram- Karl Pearson Coefficient of Correlation- Rank Correlation, Regression Chapter - 10 Sections 10.1-10.7 (omit sections10.5 \& 10.7.6)

## BOOK FOR STUDY

S.C. Gupta and V.K. Kapoor, Elements of Mathematical Statistics, Third Edition, Sultan Chand \& Sons.

## BOOKS FOR REFERENCE

1. Dr.P.R.Vittal, Mathematical Statistics,Marghaum Publications
2. S.C. Gupta and V.K. Kapoor,Fundamentals of Mathematical Statistics, Sultan Chand \& Sons
3. Goon Gupta A.M and Das Gupta, Fundamentals of Statistics, 1994,The World Press Private Limited, Calcutta
4. J.N.Kapur and H.C.Saxena, Mathematical Statistics,1999, S.Chand and Company Ltd., New Delhi.

## OUTCOME OF LEARNING

Students will be able to

- Solve the real life problems using the concepts of probability and conditional probability.
- Understand the concepts of random variables, probability distribution and its function, expected value, variance, moments and its generating functions to establish the distribution of linear combinations of independent random variables.
- Recognize the importance and value of mathematical and statistical thinking, training, and approach to problem solving, on a diverse variety of disciplines.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> ALLIED II PAPER I - STATISTICAL METHODS AND THEIR APPLICATIONS-I 

(For Computer Science Students)
(For the students admitted from the year 2019-2020)

```
HOURS/WEEK : 6
SEMESTER : III
CREDITS : 5
SUBJECT CODE: 19AAX
```


## OBJECTIVE

To apply Statistical methods for Mathematical problems and enhance the methodology to analyze data. To impart ideas of basic concepts of classification, tabulation, diagrammatic representation and measures of averages of data in statistics.

## UNIT I

Nature and Scope of Statistical methods and their limitations - Frequency Curves - Ogives Measures of Central tendencies.
Chapter-1, 2 (2.1-2.9) .
UNIT II
Measures of dispersion - Moments, Skewness and Kurtosis.
Chapter-3 : 3.1-3.12 (omit 3.7.1-3.7.3, 3.9.2-3.9.4)

## UNIT III

Probability of an event - Addition \& Multiplication theorems - Conditional probability Baye's theorem - Random variables - Distribution function - Discrete and continuous Random variable - Binomial, Poisson, uniform, normal and exponential distributions (definitions only) - Fitting of Binomial and Poisson distributions.
Chapter - 4 , Chapter -5: 5.1-5.4, Chapter-7: 7.2,7.3, Chapter-8: 8.1,8.2, 8.6

## UNIT IV

Mathematical Expectation - Moments of a random variable - Moment generation function Chebychev's inequality - Simple problems.
Chapter -6: 6.1-6.9, 6.12

## UNIT V

Correlation Coefficient, Correlation coefficient for bi-variate distributions - Scatter diagram Regression coefficients and regression lines - Rank correlation coefficient.
Chapter - 10: 10.1-10.7.4

## BOOK FOR STUDY

S.C. Gupta and V.K. Kapoor, Elements of Mathematical Statistics, Third Edition, Sultan Chand \& Sons.

## BOOKS FOR REFERENCE

1. Dr.P.R.Vittal, Mathematical Statistics,Marghaum Publications
2. S.C. Gupta and V.K. Kapoor,Fundamentals of Mathematical Statistics, Sultan Chand \& Sons
3. Goon Gupta A.M and Das Gupta, Fundamentals of Statistics, 1994,The World Press Private Limited, Calcutta
4. J.N.Kapur and H.C.Saxena, Mathematical Statistics,1999, S.Chand and Company Ltd., New Delhi.

## OUTCOME OF LEARNING

Students will be able to

- Analyze Statistical data, Compute Binomial, Poisson, uniform, normal and exponential distributions
- Find the Correlation \& Regression coefficients.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 <br> B.Sc. - MATHEMATICS <br> NON MAJOR ELECTIVE I - DESCRIPTIVE STATISTICS 

(For the students admitted from the year 2019-2020)
SEMESTER : III
CREDITS : 2
SUBJECT CODE: 19NA1

## OBJECTIVE

To impart ideas of basic concepts of classification, tabulation, diagrammatic representation and measures of averages of data in statistics.

UNIT I
Introduction of Statistics - Classification and Tabulation of data.
Chapter: 3

## UNIT II

Diagrammatic representation of data - Bar, Pie diagrams, Pictogram, Graphical representations of data.
Chapter: 4
UNIT III
Measures of averages - Arithmetic mean, Geometric mean, Harmonic mean, weighted arithmetic mean - Problems.
Chapter: 5 (Pg.: 50-55)
UNIT IV
Median, Mode- Problems.
Chapter: 5 (Pg.: 55-74)

## BOOK FOR STUDY

P.R. Vittal, Business Statistics, Margham Publications.

## OUTCOME OF LEARNING

Students will be able to

- Analyze Statistical data and known to represent diagrammatically
- Find the different measures of averages.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER VII - MECHANICS - I 

(For the students admitted from the year 2019-2020)

HOURS/WEEK : 4
CREDITS : 4

SEMESTER : IV
SUBJECT CODE: 19CAG

## OBJECTIVE

To develop the ability to visualize, formulate and solve problems in Statics. To develop the capacity to predict the effects of force while carrying out the creative design function.

## UNIT I

Forces: Forces - Types of forces - Resultant of two forces on a particle-Resultant of three forces related to a triangle acting at a point - Resultant of several forces acting on a particle-Simple problems.
Chapter 2: Sections 2.1, 2.2

## UNIT II

Equilibrium of a particle: Equilibrium of a particle under three forces - Equilibrium of a particle under several forces -simple problems. Moment of a force - General motion of a rigid bodyEquivalent ( or Equipolant) system of forces - Parallel forces - forces along the sides of a triangle couples - Simple problems.
Chapter 3: Sections 3.1 and Chapter 4: Sections 4.1 to 4.6

## UNIT III

Forces on a rigid body: Resultant of several coplanar forces - Equation of the line of action of the resultant - Equilibrium of a rigid body under three coplanar forces - Simple problems.
Chapter 4: Sections 4.7-4.9

## UNIT IV

Centre of Mass: Centre of mass-finding mass center (not using integration)- Finding mass centre using integration- Mass centre of a non-homogeneous solid - Moment of mass - Simple problems.
Chapter 6: Section 6.1-6.2

## UNIT V

Hanging String: Equilibrium of a uniform homogenous string - Sag, Suspension bridge Simple Problems.
Chapter 9: Section 9.1, 9.2

## BOOK FOR STUDY

P. Duraipandian and others, Mechanics, 2010 Edn., S. Chand Company Ltd.

## BOOKS FOR REFERENCE

1. K. Viswanath Naik and M.S. Kasi, Statics, Emerald Publishers.
2. A.V. Dharmapadham, Statics, S. Viswanathan Publishers.
3. S. Narayanan and others, Statics, S. Chand Company Ltd.
4. M.K.Venkatraman, A text book on Dynamics, 2001, Agasthiar Publication, Trichy.

## OUTCOME OF LEARNING

Students will able to

- Get the knowledge about Component of a Force, Coplanar forces, like and unlike parallel forces, Moment of a force and Couple with examples, Parallelogram of Forces, Triangle of Forces, Converse of the Triangle of Forces, Polygon of Forces which were help the students in their daily life.
- Find the resultant of coplanar couples, equilibrium of couples and the equation to the line of action of the resultant.
- Understand the knowledge about suspension Bridge through Hanging strings.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER VIII - PROGRAMMING IN 'C' THEORY 

(For the students admitted from the year 2019-2020)

HOURS/WEEK : 4
CREDITS : 4

SEMESTER : IV
SUBJECT CODE: 19CAH

## OBJECTIVE

To improve logical thinking and better understanding of programming techniques. To develop programming skill in the computer language C .

## UNIT I

Constants, Variables, Data Types And Operators: Introduction, character set, C tokens, keywords and identifiers,Constants, Variables, Data types, Declaration of variables, Assigning values to variables - Arithmetic, Relational, Increment and Decrement, Conditional operators.
Chapter- 2 Sections: 2.1-2.10; Chapter- 3 Sections: 3.1-3.7

## UNIT II

Expressions, Input and Output Operators: Arithmetic expressions, evaluation of expressions, precedence of arithmetic operators -Reading a character, Writing a character, Formatted input and output.
Chapter-3 Sections: 3.10-3.12; Chapter- 4 Sections 4.1-4.5

## UNIT III

Decision Making (Branching and Looping): Introduction,Decision making with if statement, simple if statement, the if...else statement, nesting of if... else statements, the else if ladder, the switch statement. The ?: operator, the goto statement. The while, do, for statements, Jumps in loops.
Chapter - 5 Sections 5.1-5.9; Chapter - 6 Sections: 6.1-6.5

## UNIT IV

Arrays, Character Arrays and Strings: Introduction one-dimensional, two-dimensional arrays, declaring and initializing them and string variables and Multi-dimensional arrays.

## Chapter-7 Sections 7.1-7.7; Chapter -8 Sections: 8.1, 8.2

## UNIT V

User-Defined Functions: Introduction, need for user-defined function, a multi-function program, elements of user-defined functions, definition of functions, return values and their types, function calls, function declaration, category of functions, no arguments and no return values, arguments but no return values, arguments with return values, no arguments but returns a value, functions that return multiple values, nesting of functions, recursion. Passing arrays and strings to functions, the scope, visibility and life time of variables in functions.
Chapter - 9 Sections: 9.1-9.19.

## BOOK FOR STUDY

E.Balaguruswamy, Programming in ANSIC, 6th edition, Tata-Mcgraw Hill Publishing.co

## BOOKS FOR REFERENCE

1. Ananthi Sheshasayee, Programming in $C$ with Practical, Margham Publications.
2. H. Schildt, Obsborne,Teach Yourself C, McGraw Hill. New York.
3. Mullish Cooper, The Spirit of C-An Introduction to Modern Programming, 1998, Jaico Publishing House, Delhi.
4. Yashavantkanetkar, Let us $C, 16^{\text {th }}$ edition, BPB publication.
5. Dr.P.Rizwan Ahmed, Programming in C, 2016, Margham Publications.

## OUTCOME OF LEARNING

Students will be able to

- Create algorithm to solve simple programming problems
- Design, implement and test programs that use loops, arrays, strings and functions.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> ALLIED II PAPER II - MATHEMATICAL STATISTICS -II <br> (For the students admitted from the year 2019-2020) 

```
HOURS/WEEK : }
SEMESTER : IV
CREDITS :5 SUBJECT CODE: 19AAD
```


## OBJECTIVE

This course aims to give the mathematical foundations of statistical inference.

## UNIT I

Standard discrete distributions - Binomial and Poisson distribution- Fitting of Binomial and Poisson distribution.
Chapter - 7 Sections: 7.1, 7.2 (7.2.1, 7.2.2, 7.2.6, 7.2.7), 7.3(7.3.1, 7.3.2, 7.3.9)

## UNIT II

Standard Continuous distributions - Uniform, Normal- Characteristics- Momemt generating function - Moments - Area Property - Fitting of Normal disribution - Exponential distribution.
Chapter -8 Sections: 8.1, 8.2 (8.2.1, 8.2.2, 8.2.5, 8.2.7, 8.2.11, 8.2.14) \& 8.6.

## UNIT III

Sampling Introduction- Types of Sampling-Parameter and Statistic- Sampling Distribution- Standard error-Test of significance-Null hypothesis-Alternative hypothesis-Type I \& Type II errorsCritical region and level of significance - Test of Significance of Large samples - Test of significance for single proportion, difference of two proportions, single mean, difference of two means.
Chapter - 12 Sections: 12.1-12.14(omit sections 12.10, 12.11\&12.15).

## UNIT IV

Small Sample Tests -Exact test based on $\chi^{2}$ distribution - Test of Independence of Attributes, Test of Goodness of fit - Exact test based on $t$ and $F$ distributions with regard to mean, variance and correlation coefficient
Chapter - 13 Sections: 13.1\&13.5(omit 13.5.1),
Chapter - 14 Sections: $14.1,14.2$ (14.2.6, 14.2.7, 14.2.8), 14.3

## UNIT V

Analysis of Variance - one way classification - Two way classifications - Design of experiments.
Chapter-17 \& 18
BOOK FOR STUDY
S.C. Gupta and V.K. Kapoor, Elements of Mathematical Statistics, Third Edition, Sultan Chand \& Sons.

## BOOKS FOR REFERENCE

1. Dr.P.R.Vittal, Mathematical Statistics,Marghaum Publications.
2. S.C. Gupta and V.K. Kapoor, Fundamentals of Mathematical Statistics,Sultan Chand \& Sons.
3. Goon Gupta A.M and Das Gupta, Fundamentals of Statistics, 1994,The World Press Private Limited, Calcutta
4. J.N.Kapur and H.C.Saxena,Mathematical Statistics, 1999, S.Chand and Company Ltd., New Delhi.

## OUTCOME OF LEARNING

Students will be able to

- Identify discrete and continuous distributions and apply them in simple cases.
- Handle parametric testing problems for large and small samples.
- Recognize the importance and value of mathematical and statistical thinking, training, and approach to problem solving, on a diverse variety of disciplines.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS 

ALLIED II PAPER II - STATISTICAL METHODS AND THEIR APPLICATIONS-II
(For Computer Science Students)
(For the students admitted from the year 2019-2020)

## HOURS/WEEK : 6

CREDITS : 5

## SEMESTER : IV

SUBJECT CODE: 19AAY

## OBJECTIVE

To apply Statistical methods for Mathematical problems.

## UNIT I

Sampling and Sample Designs: Theoretical Basis of Sampling - Methods of Sampling - Size of sample - Merits and Limitations of Sampling - Tests of Significance - Procedure and testing hypothesis - Standard error and sampling Distribution.
Chapter-12: 12.1-12.12

## UNIT II

Tests of significance for Large Samples.
Chapter-12: 12.12-12.15

## UNIT III

Tests of significance for Small Samples using $t$ and $F$ test of significance of coefficients of correlations.
Chapter - 14

## UNIT IV

Chi-square tests - Ttest of goodness of fit and tests of independence of attributes.
Chapter - 13

## UNIT V

Analysis of Variance: One way and Two way classification models.

## Chapter-17

BOOK FOR STUDY
S.C. Gupta and V.K. Kapoor, Elements of Mathematical Statistics, $3^{\text {rd }}$ Edn, Sultan Chand \&Sons.

## BOOKS FOR REFERENCE

1. Dr.P.R.Vittal, Mathematical Statistics, Marghaum Publications
2. S.C. Gupta and V.K. Kapoor,Fundamentals of Mathematical Statistics, Sultan Chand \& Sons
3. Goon Gupta A.M and Das Gupta, Fundamentals of Statistics, 1994,The World Press Private Limited, Calcutta
4. J.N.Kapur and H.C.Saxena, Mathematical Statistics,1999, S.Chand and Company Ltd., New Delhi.

## OUTCOME OF LEARNING

Students will be to understand the Statistical methods for Mathematical problems and developed their skills to solve the problems.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> NON MAJOR ELECTIVE II - FUNCTIONAL STATISTICS 

(For the students admitted from the year 2019-2020)

HOURS/WEEK : 2
CREDITS : 2

SEMESTER : IV
SUBJECT CODE: 19NA2

## OBJECTIVE

To impart ideas of basic concepts of index numbers, correlation and regression in statistics.

## UNIT I

Index numbers: Uses of Index Numbers - Unweighted Index Numbers.
Chapter: 13 (Pg: 536 -548)

## UNIT II

Weighted Index Numbers.
Chapter: 13 (Pg: 548-557)

## UNIT III

Correlation: Bivariate Distribution, Scatter diagram, Karl Pearson Coefficient of Correlation.
Chapter: 10 (Pg: 390-410)

## UNIT IV

Rank correlation and regression lines: Rank correlation, Repeated rank correlation, Regression lines x on y and y on x .
Chapter: 10 (Pg: 416 - 424)
Chapter: 11 (Pg: 457-467)

## BOOK FOR STUDY

P.R.Vittal, Mathematical Statistics, Margham Publications.

## BOOKS FOR REFERENCE

1. S. P. Gupta, Practical Statistics,2006, Sultan Chand \& Sons, New Delhi.
2. MODE, E. B.,Elements of Statistics, Prentice Hall
3. S.P. Gupta, Statistical Methods (for CA intermediate), Sultan Chand \& Sons.

## OUTCOME OF LEARNING

Students will be to

- Understand the basic concepts and uses of Index numbers.
- Find the Correlation \& Regression coefficients.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER IX - ABSTRACT ALGEBRA - I <br> (For the students admitted from the year 2019-2020) 

HOURS/WEEK : 6
CREDITS :5

SEMESTER : V
SUBJECT CODE: 19CAJ

## OBJECTIVE

To provide a first approach to Algebra which lays foundation for modern mathematics. To focus on the study of certain structures called groups, rings, fields and some related structures and also to develop proof-writing skills.

## UNIT I

Definition of a Group - Some Examples of Groups - Some Preliminary Lemmas - Subgroups. Chapter 2: 2.1-2.4.
UNIT II
A counting Principle - Normal Subgroups and Quotient groups- Homomorphisms.
Chapter 2: 2.5-2.7 (Omit Applications 1 and 2 of 2.7).

## UNIT III

Automorphisms - Cayley's Theorem - Permutation Groups.
Chapter 2: 2.8-2.10.
UNIT IV
Definition and Examples of Rings - Some special Classes of Rings - Homomorphism - Ideals and Quotient Rings.

## Chapter 3: 3.1-3.4.

## UNIT V

More Ideals and Quotient Rings - Field of quotients of Integral domain - Euclidean rings.
Chapter 3: 3.5-3.7.

## BOOK FOR STUDY

I.N.Herstein, Topics in Algebra, 2 ${ }^{\text {nd }}$ Edition, John Wiley \& Sons, 2011.

## BOOKS FOR REFERENCE

1. John B. Fraleigh, AFirst Course in Abstract Algebra, 7th Ed., Pearson, 2013.
2. David S. Dummit \& Richard M.Foote, Abstract Algebra, 3 rd Edition, Wiley India Pvt.Ltd, 2003.
3. J.J. Rotman,Advanced Modern Algebra, $2^{\text {nd }}$ Edition, Graduate Studies in Mathematics, Vol. 114, AMS, Providence, Rhode Island, 2010.
4. J.Gallian, Contemporary Abstract Algebra, 8th Edition, Brooks/Cole,Cengage learning, 2012.
5. Qazi Zameeruddin\&Surjeet Singh,Modern Algebra, 8th Edition Vikas Publishing,2006.
6. www.ime.usp.br/~aholguin/LIVROS/Beachy.pdf.

## OUTCOME OF LEARNING

Students will be able to

- Understand the connection and transition between previously studied mathematics and more advanced mathematics.
- Understand the elementary concepts of rings and fields and appreciate the similarities and differences between these concepts and those of group theory.


# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER X - REAL ANALYSIS - I <br> (For the students admitted from the year 2019-2020) 

HOURS/WEEK : 6
CREDITS : 5

SUBJECT CODE: 19CAK

## OBJECTIVE

To provide a comprehensive idea about real number system, convergence and divergence of sequences, series and to focus on limits in metric space this lays a foundation for analysis.

## UNIT I

Sets and Functions: Sets and elements - Operations on sets - Functions - Real valued functions - Equivalence - Countability - Real numbers - Least upper bounds.

Chapter 1: Sections 1.1 to 1.7

## UNIT II

Sequence of real numbers: Definitions of sequence and subsequence - Limit of a sequence Convergent sequences - Divergent sequences - Bounded sequences - Monotone sequences Operations on convergent sequences - Operations on divergent sequences.

## Chapter 2: Sections 2.1 to 2.8

## UNIT III

Sequence and Series of real numbers: Limit superior and Limit inferior - Cauchy sequences Convergence and divergence - Series with non-negative terms - Alternating series.
Chapter 2: Sections 2.9 to 2.10, Chapter-3: Sections-3.1 to 3.3

## UNIT IV

Series of real numbers: Conditional convergence and absolute convergence - Tests for absolute convergence - Series whose terms form a non-increasing sequence - The class $l^{2}$.
Chapter 3: Sections 3.4, 3.6, 3.7 and 3.10

## UNIT V

Limits, Metric spaces and Continuous functions on Metric Spaces: Limit of a function on the real line - Metric spaces - Limits in metric spaces - Functions continuous at a point on the real line, reformulation, and functions continuous on metric spaces.
Chapter 4: Sections 4.1 to 4.3, Chapter 5: Sections 5.1 to 5.3.

## BOOK FOR STUDY

Richard Goldberg, Methods of Real Analysis, Oxford and IBH Publishing, 1970.

## BOOKS FOR REFERENCE

1. Dr. K. Chandrasekara Rao and Dr. K.S. Narayanan, Real Analysis, Vol.1, S. Viswanathan printers \& publishers Pvt. Ltd.
2.Tom M.Apostol, Mathematical Analysis,2nd Edition, Addison-Wesley New York, 1974.
2. Bartle, R.G. and Shebert, Real Analysis,John Wiley and Sons Inc., New York, 1976.

## OUTCOME OF LEARNING

Students will be in the position to appreciate the beauty of the subject which serves as a stepping stone into the idea of abstract topological spaces.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 <br> B.Sc. - MATHEMATICS <br> CORE PAPER XI - MECHANICS - II <br> (For the students admitted from the year 2019-2020) 

HOURS/WEEK: 6
CREDITS : 5

SEMESTER : V
SUBJECT CODE: 19CAL

## OBJECTIVE

To introduce the concept of forces acting on moving objects and to understand their effect on velocity and acceleration. Further the concepts of smooth surfaces and their impacts, projectiles are introduced. Central orbits and moment of inertia are also dealt in detail to help in developing different designs.

## UNIT I

Kinematics: Velocity - Resultant of $\mathrm{v}_{1}$ and $\mathrm{v}_{2}$ - Resultant Velocity - Acceleration - Velocity and acceleration in a rectilinear motion - Velocity and acceleration in a coplanar motion - Angular velocity - Relative angular velocity - Rectilinear motion when the acceleration is constant - Simple Harmonic Motion - Simple problems.

## Chapter 1: Sections 1.2 to 1.4, Chapter 12: Section 12.1-12.3 only

## UNIT II

Impact: Impulsive force - Impulse - Conservation of linear momentum - Impact of two smooth spheres - Direct impact of two smooth spheres - Impact of a smooth sphere on a fixed smooth plane Oblique impact between two smooth spheres - Simple problems.
Chapter 14: Sections 14.1 to 14.5

## UNIT III

Projectile: Forces on a projectile - Nature of a trajectory - Results pertaining to the motion of a projectile - Maximum horizontal range for a given velocity -Two trajectories with a given speed and a range-Projectile projected horizontally -Projectile projected on an inclined plane - Maximum range on an inclined plane.
Chapter 13: Sections 13.1, 13.2

## UNIT IV

Central Orbits: Central force and Central orbit - Differential equation of a Central orbit - Laws of a central force - Methods to find the central orbits - Kepler's laws on Planetory motion - Simple problems.

## Chapter 16: Sections 16.1 to 16.3

## UNIT V

Moment of Inertia: Moment of Inertia - Theorems of parallel and perpendicular axes - M.I. of a triangular lamina, circular lamina, elliptic lamina, circular ring, right circular cone, sphere(hollow and solid) and rod.
Chapter 17: Section 17.1

## BOOK FOR STUDY

P. Duraipandian, Mechanics, S. Chand Company Ltd., 2010.

## BOOKS FOR REFERENCE

1. A.V. Dharmapadham, Dynamics, S. Viswanathan Publishers.
2. M.K. Venkatraman, A Text Book on Dynamics, 2001, Agasthiar Publications.
3. S.G Venkatachalapathy, Dynamics,Margham Publications.

## OUTCOME OF LEARNING

Students will be able to understand the concept of forces acting on moving objects, velocity and acceleration, impacts, projectiles, central orbits, moment of inertia which helps in developing different designs.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER P1 - PROGRAMMING IN C PRACTICAL 

(For the students admitted from the year 2019-2020)

```
HOURS/WEEK: }
    SEMESTER : V
CREDITS :5
SUBJECT CODE: 19CA1
```


## OBJECTIVE

To provide strong logical thinking and error free syntax code writing to master the debugging techniques and to present the results in neat form in C language.

UNIT - I:
To write and run the programs for the following problems:
To find the square of numbers from 1 to 20 using

1. For Loop.
2. While loop
3. Do-While loop
4. Go to statement

To generate the series for the following functions and to check the result using the corresponding builtin functions:

1. $\operatorname{Sin} x$
2. $\quad \operatorname{Cos} x$
3. $\mathrm{e}^{\mathrm{x}}$

To count the number of vowels, consonants, words, whitespaces in a line of text and array of lines.
To reverse a string and check for the palindrome.

## UNIT - II:

To enter two numbers and print all the prime numbers between them.
To compute the following using recursion and ternary operator.

1. The factorial of a number.
2. Binomial coefficient nCr where n and r are positive integers.
3. The $\mathrm{n}^{\text {th }}$ Fibonacci number from the Fibonacci series where n is an integer.

To perform:

1. Matrix addition and subtraction.
2. Matrix multiplication
3. Transpose of a matrix.
4. Determinant of a matrix.

To sort a given set of numbers in the ascending order by

1. Insertion sort.
2. Bubble sort.
3. Selection Sort.

## UNIT - III:

To solve Algebraic and transcendental equations by

1. Bisection Method.
2. Newton Raphson Method.

Simple Problems:
To solve a system of linear simultaneous equations by Gauss Elimination Method.

## UNIT - IV:

Simple problems:

1. To Interpolate using Lagrange's Formula for interpolation.
2. To Evaluate a definite integral using Simpson's one-third rule
3. To Solve an Ordinary Differential equation of first order by Runge-Kutta method of fourth order.

## BOOKS FOR REFERENCE

1. E. Balagurusamy, Programming in ANSI C, $2^{\text {nd }}$ edition, Tata Mcgraw hill co., 1996.
2. Ananthi Sheshasayee, Programming in C with Practicals,Margham Publications.
3. V. Rajaraman, Computer Oriented Numerical Methods, $3^{\text {rd }}$ Edition, Prentice Hall of India.
4. Mullish Cooper, The spirit of C, Indian edition by Jaico publisher, 1987.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> ELECTIVE PAPER I - OPERATIONS RESEARCH - I <br> (For the students admitted from the year 2019-2020) 

## HOURS/WEEK : 6

CREDITS : 5

SEMESTER : V
SUBJECT CODE: 19EAA

## OBJECTIVE

To develop computational skill and logical thinking in formulating industry oriented problems as a mathematical problem and finding solutions to these problems. To understand the concept of solving the Linear Programming Problems and application to transportation, assignment, job sequencing and game theory.

## UNIT I

LPP \& Formulation: Introduction to OR-Definition - Scope - Phase - Limitations of OR- Types of models - Linear Programming: Formulation - Graphical method of solution.

## Chapter- 1, 2 and 3

UNIT II
The Simplex method: Simplex algorithm - Simplex computational procedure - Artificial variables - Charne's method of penalties

## Chapter- 4 except two phase method (4.1-4.5)

## UNIT III

Transportation Problem: Application and solution of transportation problems - Degeneracy in transportation problems - Unbalanced transportation problems.

## Chapter- 10.1-10.13

UNIT IV
Assignment Problem: Assignment algorithm-solution of assignment Problems - Unbalanced assignment problems. Travelling salesman problem. Sequencing: Sequencing problem with (i) n jobs and two machines, (ii) n jobs and three machines, (iii) n jobs and m machines. Two jobs through m machines (Graphical solution)
Chapter- 11.1-11.4, 11.7, 12.1-12.6
UNIT V
Two person zero sum games - The Maximin-Minimax Principle - Games without saddle points

- Mixed Strategies - Graphical solution of $2 \times n$ and $m \times 2$ games - Dominance property.

Chapter-17.1-17.7

## BOOK FOR STUDY

Kanti Swarup, P.K. Gupta, Man Mohan, Operations Research, $9^{\text {th }}$ Edition, Sultan Chand \& Sons.

## BOOKS FOR REFERENCE

1. Gupta P.K and D.S. Hira, Operations Research, S Chand and Company
2. Prof.Dr.V.Sundaresan,K.S.GanapathySubramanianand K.Ganesan, Resource Management Techniques, A.R.Publications.
3. S.K. Mittal \&B.S Goel, Operations Research,Pragati Prakashan, Meerut.

## OUTCOME OF LEARNING

Students will be able to develop computational skill and logical thinking in formulating linear Programming Problems and solving them. They have also learnt the applications to transportation, assignment, job sequencing and game theory.

```
BHARATHI WOMEN'S COLLEGE(AUTONOMOUS)CHLNNA1-600 308,
    CORE ELECTIVEPSOMERTHEMATICS
        (For the students admitted fomFRICAL, ANALYSIS
FWEEK:6
MIS+5
```

TiUIVE
in of ordinary and partial differitting to the studens and it's applications with mumertical: The solution of nonlinear equations $\mathrm{f}(\mathrm{x})=0$. The solution of linear sysum $\mathrm{AX}=\mathrm{B}$
Chapter $2: \sec 2.1$ to 2.4 , and $2.6-2.7$
Chapter 3 : sec 3.3 to 3.7

A11:
Chinpolation and polynomial approximation - Curve fitting.
Chapter $5: \sec 5.1$ to 5.2
NIII: Numerical differentiation - Numerical integration.
Chapter $6: \sec 6.1,6.2$
Chapter $7: \sec 7.1$ to 7.2
NII IV: : Solution of ordinary differential equations
Chapter $9: \sec 9.1$ to 9.6
INT Y : Solution of partial differential equations
Chapter 10: $\sec 10.1$ to 10.3

## P00K FOR STUDY

Numerica! Merhods for Mathematics, Science and Engineering- John H.Matheus, 2rd edition, Prentice Hall, New Delhi. 2003.

## 300KS FOR REFERENCE

1. Conte S.D and Carl de Boor (1980)- Elementary Numerical Analysis. An Agorithmic Approach, Mc.Graw Hill, New York.
2. Janes B. Scarborough- Numerical Mathematical Analysis, Sixth Edition, Oxford \& IBH Publishing Co. Pvt. Ltd., New Delhi.

## OTTCOME OF LEARNING:

ealytically.

```
BHARATHI WOMEN'S COLLEGE(ANTONOMOUSKCHENNAI-600 108.
B.SE-MATHEMATICS
    CORE ELECTIVE PAPEREMATICS
R/ WEEK: 6
(IS: 5
    (For the students admited from GRAPH THEORY
```



```
                                    SEMESTER :V
                                    SUBAECT COHE: 19EAC
```

CIVES: This course introduces P
त101: INTRODUCTION TO GRAPHS
phere 2 and 3
(11) PLANAR AND DUAL GRAPHS

Wiar Graphs-Kuratowski's Two Graphs-Representations of a Planar graphs-
mocion of Planarity-Gcometric Dual-Combinatorial Dual.
Qpatros 5.2-5.7.
NT-1I: MATRIX REPRESENTATION OF GRAPHS
dience Matrix-Submatrices of A(G)-Circuit Matrix-Fundamental circuit Matrix
as Rank of B -Applications to switching netwerk.
diplet 7. 7.1-7.5.
MII IV: COLOURING ,COVERING AND PARTITIONING
(urmatic Number-Chromatic partitioning-Chromatic polynomial-Matchings.
Ihyler 8: 8.1-8.4.
NII-V: DIRECTED GRAPHS
hrexed graph - Types of Digraphs - Digraphs and Binary Relations - Directed Paths ad Connectedness - Euler Digraphs. Fundamental circuits in Digraphs -Adjacency
lutix of a Digraphs.
Therrer 9:9.1-9.8.

## DOK EOR STUDY:

Xaringh Deo -Graph Theory with applications to Engineering and Computer Science PHI Learning Pvt.Ltd. 2019.

## 30KS FOR REFERENCE:

1 Choudum.S.A. - A First Course In Graph Theory, Macmillan India Limited, 1987.
I Arumugam.S and S. Ramachandran, - Invitation to Graph Theory. Scitech publications India Pvt. Limited, Chennai - [2001, Edition].
ficome of Learving:
Students will able to acquire knowledge in basic concepts in graph theory and its applications.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER XII - ABSTRACT ALGEBRA - II 

(For the students admitted from the year 2019-2020)

HOURS/WEEK: 6
SEMESTER : VI
CREDITS : $\mathbf{5}$
SUBJECT CODE: 19CAM

## OBJECTIVE

To master the properties of transformations between vector spaces and understand how they are connected with matrices in linear transformations. To determine the dimension of spaces associated with matrices and linear transformations.

## UNIT I

Vector Spaces-Elementary Basic Concepts - Linear independence and Bases.

## Chapter 4: 4.1 and 4.2.

## UNIT II

Dual Spaces - Inner product spaces.
Chapter 4: 4.3 and 4.4.
UNIT III
The algebra of linear transformations- Minimal polynomial - Regular and singular transformations - Rank of a linear transformation.

## Chapter 6: 6.1

UNIT IV
Characteristic roots - Matrices.
Chapter 6: 6.2 and 6.3.
UNIT V
Canonical forms - Triangular form.
Chapter 6: 6.4.

## BOOK FOR STUDY

I.N.Herstein, Topics in Algebra, ${ }^{\text {nd }}$ Edition, John Wiley \& Sons, 2011.

## BOOKS FOR REFERENCE

1. P.B. Bhattacharya, S.K. Jain, S.R. Nagpaul, First Course in Linear Algebra, 2nd Edition, Cambridge University Press, 1994.
2. Kenneth M Hoffman and Ray Kunze, Linear Algebra, $2^{\text {nd }}$ Edition, Prentice-Hall of India Pvt. Ltd, New Delhi, 2013.
3. J.J. Rotman, Advanced Modern Algebra, $2^{\text {nd }}$ Edition, Graduate Studies in Mathematics, Vol. 114, AMS, Providence, Rhode Island,2010.
4. John B. Fraleigh, A First Course in Abstract Algebra,7th Ed., Pearson, 2002.

## OUTCOME OF LEARNING

Students will be able to find the matrix representation of a linear transformation given bases of the relevant finite dimensional vector spaces.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER XIII - REAL ANALYSIS - II <br> (For the students admitted from the year 2019-2020) 

HOURS/WEEK : 6
CREDITS : 5

SUBJECT CODE: 19CAN

## OBJECTIVE

To learn the fundamentals of continuity, connectedness, completeness, compactness in metric spaces and to study about Riemann integration, application of Rolle's theorem and Taylor's theorem.

## UNIT I

Continuous functions on metric spaces: Open sets - closed sets - Discontinuous functions on the real line.

## Chapter 5: Sections-5.4 to 5.6

## UNIT II

Connectedness and Completeness: More about open sets - Connected sets - Bounded sets and totally bounded sets - Complete metric spaces.

## Chapter -6: Sections 6.1 to 6.4

## UNIT III

Compactness: Compact metric spaces - Continuous functions on a compact metric spaces Continuity of the inverse functions - Uniform continuity.
Chapter 6: Sections-6.5 to 6.8

## UNIT IV

Calculus: Sets of measure zero - Definition of the Riemann integral - Existence of the Riemann integral (Statement only) - Properties of the Riemann integral - Derivates - Rolle's theorem - , The law of the mean - Fundamental theorem of calculus.

## Chapter 7: Sections 7.1 to 7.8

## UNIT V

Taylor Series \& Sequence and Series of functions: Taylor's theorem- Point wise convergence of sequences of functions - Uniform convergence of sequences of functions.
Chapter 8: Section 8.5 only and Chapter 9: Sections 9.1 and 9.2

## BOOK FOR STUDY

Richard R. Goldberg, Methods of Real analysis, Oxford \& IBH Publishing, 1970.

## BOOK FOR REFERENCE

1.Tom M.Apostol, Mathematical Analysis,2nd Edition, Addison-Wesley New York, 1974.
2.R. Bartle and Sherbert,Real Analysis, $5^{\text {th }}$ Edn., Wiley and Sons.

## OUTCOME OF LEARNING

Students will be able to gain knowledge about the nature of functions, differentiation and Riemann integration and its application.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> CORE PAPER XIV - COMPLEX ANALYSIS <br> (For the students admitted from the year 2019-2020) 

HOURS/WEEK : 6
CREDITS :5

SEMESTER : VI
SUBJECT CODE: 19CAP

## OBJECTIVE

To introduce the fundamental ideas of the functions of complex variables and developing a clear understanding of the concepts of complex analysis this will allow students to work effectively.

## UNIT I

Analytic Functions: Introduction to Functions of a complex variable, Limits, Continuity, Derivatives. Cauchy- Riemann equations - sufficient conditions for Differentiability - polar coordinates - Analytic functions - Examples - Harmonic functions
Chapter 2: Sec 12, 15, 18, 19, 21 - 26.

## UNIT II

Integrals: Definite integrals of functions - Contours - Contour integrals - Some examples Antiderivatives - Cauchy's Goursat Theorem (Statement only) - Cauchy's integral formula - An extention of the Cauchy's integral formula - Some consequences of the extension - Liouville'sTheorem and Fundamental Theorem of algebra - Maximum modulas principle.
Chapter 4: Sec 38-41, 46, 50-54.

## UNIT III

Power Series: Taylor series - examples - Laurent series - examples - Absolute and Uniform convergence of power series - Continuity of sums of power series.

## Chapter 5: Sec 57-64.

## UNIT IV

Residues and Poles: Residues - Cauchy residue theorem - The three types of isolated singular points - Residues at poles - Examples - Zeros of Analytic functions - Zeros and poles - Evaluation of improper integrals - Example - Improper integrals from Fourier analysis - Jordan's lemma (Statement only)- Definite integrals involving sines and cosines.
Chapter 6: Sec 69, 70, 72-76.
Chapter 7: Sec 78-81, 85.

## UNIT V

Mappings: Mappings - Mappings by the exponential function - Linear transformations - The transformation $\omega=1 / \mathrm{z}$ - Mappings by $1 / \mathrm{z}$ - Linear fractional transformations - An implicit form - The transformation $\omega=\sin z-$ Mappings by $z^{2}$ and Branches of $z^{1 / 2}-$ Conformal mapping - Harmonic conjugates.
Chapter 2: Sec 13, 14
Chapter 8: Sec 90-94, 96, 97.

## BOOK FOR STUDY

James Ward Brown, Ruel V.Churchill, Complex variables and Applications,Eighth Edition, McGrawHill Publications, New Delhi.

## BOOKS FOR REFERENCE

1. T.K.Manicavachagom Pillai, Dr.S.P.Rajagopalan and Dr.R.Sattanathan, Complex Analysis, S.Viswanathan Publishers Pvt. Ltd, 2008.
2. P. Duraipandian and LaxmiDuraipandian, Complex Analysis,(1976),Emerald Publishers, Chennai.
3. S. Ponnusamy, Foundations of Complex Analysis,(2000), Narosa Publishing House, New Delhi.
4. Murray R. Spiegel, Theory and Problems of Complex Variable,(2005) Tata-Mcgraw Hill Edition, New Delhi.
5. S.G.Venkatachalapathy, Complex Analysis,Margham Publications.

## OUTCOME OF LEARNING

Students will be able to understand the significance of differentiability and analyticity of complex functions leading to the Cauchy Riemann equations, mapping, Cauchy's Integral formulae, power series and classify the nature of singularity, poles and residues and application of Cauchy Residue theorem.

# BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS <br> ELECTIVE PAPER-II - OPERATIONS RESEARCH - II <br> (For the students admitted from the year 2019-2020) 

HOURS/WEEK: 6
CREDITS : 5
SEMESTER : VI
SUBJECT CODE: 19EAD

## OBJECTIVE

To understand the concepts of duality and network analysis. To study the application in replacement and inventory theory.

## UNIT I

Introduction to Duality - general primal - dual pair - formulating a dual problem - Primal dual pair in matrix form - Dual simplex method - Simple Problems.
Chapter 5 -Section: 5.1-5.4, 5.9

## UNIT II

Replacement Problem: Replacement of items that deteriorate with time-Replacement of items that fail completely.
Chapter18-Section: 18.1-18.3

## UNIT III

Network Analysis - Basic concepts - Drawing network diagrams - Critical Path method PERT - Algorithm for PERT, Difference between PERT \& CPM.
Chapter- 25 Section: 25.1-25.8

## UNIT IV

Inventory: Deterministic problems - Inventory control - Definition - Problems with (i) Uniform rate of demand, infinite rates of production no shortages, (ii) Uniform rate of demand, finite rates of replenishment no shortages, (iii) Uniform rate of demand, instantaneous production with shortages and (iv) Uniform rate of demand, instantaneous production with shortages and fixed time
Chapter 19: Section: 19.1-19.11

## UNIT V

Probabilistic Models - Newspaper boy problem - Discrete and continuous type cases. Inventory control with one price break and two price breaks.

## Chapter- 19.12

## BOOK FOR STUDY

Kanti Swarup, P.K. Gupta, Man Mohan, Operations Research, $9^{\text {th }}$ Edition, Sultan Chand \& Sons.

## BOOKS FOR REFERENCE

1. Gupta P.K and D.S. Hira, Operations Research, S Chand and Company

2 .Prof V.Sundaresan, K.S.Ganapathy Subramanian and K.Ganesan, Resource Management Techniques, A.R.Publications.
3.S.K. Mittal \&B.S Goel, Operations Research, Pragati Prakashan, Meerut.
4.A.Rahim Basha, Basic Graph Theory with Applications,Sri Hariganesh Publications LLP 1 st Edition.

## OUTCOME OF LEARNING

Students will be able to

- Apply the concepts of duality in solving LPP.
- Understand the mathematical tools and models that are needed to solve optimization problems.

```
BHARATHI WOMEN'S COLLEGE(AUTONOMOUS).CHENNA1-600.108.
p/RS/WEEK : 6
    CORE ELECTIVEPAPER PHEMATICS
        (For the students admitted FUZZY MATHEMATICS
,f%DIS : 5
                                    SEMESTER ; V1
                            SL BIECT CODE: 19EAE
```


## ECIVES:

This course introduce the basic concepts of fuzzy sets, fuzzy graphs and their relations: Whap it ains to develop the skills in solving fuzzy problems and it's applications.
NIT.1:
Chapter I: Sec. 1 to 8
NIIT-II:
Fuzzy Graphs.
Chapter II: Sec. 10 to 17
|NIT-III:
Fuzzy Relations.
Chapter II: Sec, 19 to 26
INIT-IV:
Fuzzy Logic.
Chapter III: Sec 31 to 36 and 39
NIT-V:
The Laws of Fuzry Composition.
Chapter IV: Sec. 43 to 49
BOOK FOR STUDY:
A.Kaufman, Introduction to the theory of Fuzzy subsets, Vol.1. Academic Press, New York, 1975.

BOOK FOR REFERENCE: Set Theory and its Applications, Allied Publishers, Chennai. 1996 1. H.J.Zimmermann, Fuzzy Set Theory sets and Fuzzy Logic-Theory and Applications, Prentice 2. George J. Klir and Bo Yuan,
Hall India, New Delhi, 2001

OUTCOME OF LEARNING: Students will be able to solve problems in fuzzy logic and its composition.

```
BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNA1-600 LOX. B.SE MATHEMATICS
CORE ELECTIVE PAPER - I ELEMENIARY NLMHER THEORY (For the students admitted from the ycar 2019-2020)
```

SFMESTER :VI

```
```

WWEEK:6

```
```

WWEEK:6

```
```

pITS:5

```
pITS:5
SU ILIECT CODE: 19EAF
```

SU ILIECT CODE: 19EAF

```

TIVES:
This counse introduce the bastic concepis of Congroences, Arilimetic Functions cornuph.
```

up und Ficlde

```
vIL:
cion - Divisibility - Primes - Congruence - Solation of Congruences
petar:-1.1-1.3, Chapter2 \(2: 2.1-2.2\)

NIT.II:
fincesemainder Theorem. Number Theory from an Alpehraic view
dint Groups, Rings and Fields
Chupler 2:2.2.2.2.10.2.11.
NTI-1II
vatratic Residues-Quadratic reciprocity- The Jacobi symbel.
dupler \(3: 3,1,3,2,3,3\).
INIT-IV:
Gritest integer function,Arithmetic Functions. The Mobias liversion formula.
(hupler:4:4.1-3
(NTT-Y
The simple continued fractions-Fuclidean algorithuns-Uriqueness-infinite continued
taction Chapter:7. 7.1.7.7.,7,3.

\section*{BOOK FOR STUDY}

An Introduction to the Theory of Nambers by lvanNiven. HerbertS. Zuckerman undthigh 1 Mantgomery \(5^{\text {III }}\) Edition, Wiley Student Edition, NewDelhi,1991.

\section*{300K FORREFERENCE:}
1.David N.Burton "ElementaryiNumber Theory", \(6^{\text {d }}\) Edition, Tata MeGraw HIL.L. Publishen 2008.

2Kumaravelu. S and Sushecla Kumaravelu-Elememis of Number Theory. Nugareoil. 2002.

\section*{OUTCOME OF LEARNING:}

Students acquire knowledge in basic concepts of pumber theory

\title{
BHARATHI WOMEN'S COLLEGE(AUTONOMOUS),CHENNAI-600 108 B.Sc. - MATHEMATICS \\ ELECTIVE PAPER-III - DISCRETE MATHEMATICS \\ (For the students admitted from the year 2019-2020)
}

HOURS/WEEK: 6
CREDITS : 5

SEMESTER :VI
SUBJECT CODE: 19EAG

\section*{OBJECTIVE}

To introduce logics and inference theory for understanding and applying them in real life. To familiarize students with Lattices, Boolean algebra and Graph Theory and apply logical reasoning to solve a variety of problems.

\section*{UNIT I}

Mathematical logic - statements and notations - connectives - Normal forms.
Chapter: 1 - Sections: 1.1, 1.2 (1.2.1-1.2.11 except 1.2.5), 1.3 (1.3.1-1.3.4).

\section*{UNIT II}

Theory of inference for the statement calculus -The predicate calculus.
Chapter: 1 - Sections: 1.4 (1.4.1-1.4.3), 1.5 (1.5.1-1.5.5).

\section*{UNIT III}

Lattices and Boolean Algebra- Lattices as posets - Boolean algebra - Boolean function.
Chapter: 4 -Sections: 4.1 to 4.3.

\section*{UNIT IV}

Graph theory - Basic definition - Some special simple graphs - Subgraphs - Isomorphic graphs - Matrix representation of graphs - Paths, cycles, connectivity (Excluding algorithms).
Chapter: 7 (Pg. No. 366 - 391).

\section*{UNIT V}

Eulerian and Hamiltonian graphs - Connectedness in directed graphs - Trees - Some properties of trees - spanning trees - Rooted and Binary trees - Properties of Binary trees - Tree traversals. (Excluding algorithms)
Chapter: 7 (Pg. No. 392-421).

\section*{BOOKS FOR STUDY}
1. J.P. Tremblay and R. Manohar, Discrete Mathematical Structures with Applications to Computer Science, Tata McGraw - Hill publishing company Ltd.
2. T. Veerarajan, Discrete Mathematics with Graph Theory and Combinatorics,McGraw Hill Education (India) Private Ltd.

\section*{BOOKS FOR REFERENCE}
1. Venkataraman M.K. and others,Discrete Mathematics,2000, The National Publishing Company.
2. Richard Johnsonbaugh, Discrete Mathematics,Fifth Edn., Pearson Education Asia, New Delhi .

\section*{OUTCOME OF LEARNING}

Students will be able to understand the basic principles of logic, Lattices, Boolean algebra, Graph Theory and Inference Theory to real life situations in the form of graphs.
```

BHARATHI WOMEN'S COLLEGE(ALTONOMOUS),CHENNAI-600 108.
CORE ELFESE - MATHEMLTICS
(For the students admittER - Ill ASTRONOMY
*)
GEDITS: 5
SEMESTER:VI
SU BJECT CODE: 19EAH

```
ECIIVES:

To introduce the exciting world of astronamy to the students and to help them to ofy Spherical Trigonometry, movement of Celestial objects, Kepler's lawsiand phase of moom.

Spherical Trigonometry: Spherical Triangle-The fundumental formulae of Spherical
ponometry, the sinc,cosine four parts and Napier formulac (without proof?
pupter I Pages:1-37.
ATT-II
The Celestial Sphere: Celestial coordinators - Diumal motion - Rising and setting of a stat sdereal time - Circumpolar star - Morning and Evening stars - Twilight - Earth - Length of the \$5.
(copter:II \& III Pages: 38-131.
NIT-III
Refraction - Tangent Formula - Cassini's formula - Effects of Refraction - Geocentric Pallax - Effects of Geocentric Parallax - Heliocentric Panallax - Effects of Heliocentric Parallax
Abecration - Its Effeets,
Chapter-IV \&V Pages: \(140-170\).

\section*{NIT-IV}

Kepler's Laws - Verification of Kepler's Laws - True anomaly, Mean Anomaly - Eccentric Anomaly, Relation between them - Time - Equation of Time - Seasons - Converson of Time. Chapter-VI \& VII Pages: 172-213.

\section*{UNIT-V}

The Moon - Sidereal Month. Lunation and Relation between them - Phases of the Moon Lumar Libration - Surface of the Moon - Metonic Cycle - Tides - Eclipses :- Shadow Cone Minimum and Maximum number of Eclipses,
Planetary Phenomena - Bodes law - Elongation - Sidereal Period, Synodic period and the relation between them - Phase - Stationary Points - Solar System - Stellar Universe - A bric history of Astonomy, Chapters: XII,XIII,XIV, XV XVI Pages: 334-527.
BOOKS FOR STUDY
Kumaravelu. S and Susheela Kumaravelu - Astronomy for degree classes. Purt-1 and Part-11 Rainbow printers, Nagarcoil (2005)

\section*{BOOKS FOR REFERENCE}
L. Ramachandran. G.V.- Astronomy
2. George. O.Abell - Exploration of the Uhiverse (Second Edition).

OUTCOME OF LEARNING: Students will get knowledge in analyse the various topics in astronomy.
```

BHARATHI WOMEN'S COLLEGE(ALTONOMOUS).CHENNAI-G00 I08.
BCSE - MATHEMLATICS
(For the students admitied COMBINATORINL. MATHEMATICS
OUS/WEEK:6
, DITS:5
SEMESIFR:VI
SUPHECT CODE: 19EA.J
HECTIVES: chation.
NIT-I
tations and Combinations: Introduction - The Rules of Sum and Product - Permutations
andbinations-Pascal's Identity, Vandermonde's Identity
thy tex:6. Sections: 1-4

```

NIITII
ganutation with repetition- circular permutation- pigconhole principle -genernlization of fetanlole principle.
(hapter 6: Sections: 5-7
NIT-III
Gencrating Functions: Introduction - Generating Functions of Combinations - Enumentors fee fermulations - Distributions of Distinct Objects into Non distinct Cells - Partition of Integers.
Chapter:6 Section:14
WIT-IV
Recurrence Relation: Mathematical induction- Linear Recurrence Relation with Constant Coefficients -Solution by the Technique of Gencrating Functions.
Chapter:6 Sections:11-13
UNIT-V
The Principles of Inclusion and Exclusion: Introduction - The Principle of Inclusion and Exelusion - The General Formula -Derangements -Simple Problems:
Chapter:6 Sections: 8-10

\section*{HOOK FOR STUDY:}
T. Veerarajan-Discrele mathematics with Graph thoory and Combinatorics \(\left(2^{\text {id }}\right.\) edtion) Mc(iraw - Hill Education(India) Pvt. company.

BOOKS FOR REFERENCE:
1. C.L.Liu-Introduction to Cambinatorial Mathematics, McGraw - Hill Book company. 2. Santha.S - Discrete mathematics with Combinatorics and Graph theory 2012

OUTCOME OF LEARNING: Student will able to understand the concepts of Permutations and Combinations, Generating Functions, Recurrence relation and principle of inclusion and exclusion.


\section*{B.A. iB.Sc.iA.Cym.}
```

GENERAL ENGIISH PAPER-I

```
(Fer'the stadeats admitted from the year 2019i
IIOLRS PER WEEK : CREDITS ; 3 \(\qquad\)
\(\qquad\)
\(\qquad\)

\section*{ORIECTIVES:}




\section*{UNII-I: POETRY}

2) Fhe House ol'My Casahed - Dilip Chiter

NNJT- II: PROSE

2) The Deanly Industry - Alicus Hux?

LNIT- IIt: SHOHT STORY
I) The Elind Doe - R. K. Nardyan

\section*{I!VIT-IV: GRAMMAR}
1) Terse - Identificallinn of Tense

2j Arliteles • Fith in the Blanks
3) Parts of Sipceld - Idendifatation

\section*{UNIT- Y: COMPOMSTION}
1) Readitut Comprehensjon (Textual)
2) Hints INevelispment

\section*{Horg tor sididy.}


\section*{BOOK゙S FOR REFIRRENCE:}



\section*{}

 "̈utia لirtcererat ụenres
- Posarese citbetively : funcoanonal usage of Grammai


```

                        B.A.iB.Sc.B.Com.
    $\qquad$

## ORJECJIVFS:

- T: ニni



## LNAF-I: POF,TRY

1) A Pown Troc - Will emm Balk


## ENIT- II: PROSE

1) J Wion Let Elim (\%o - Mudhavas Kuty
2) The Beautiful Ruskin Boad

## UNNIT- ISI: BIOG:RAPIFY

J) Jr. Ambedkar

## INJT- IV: GRAMBAR

1) Tensc - Wistiting Sentences
2) Article- (lloze Jest
3) Pars of Speech - Fill in the blanks with the suitable parts of speeil

## UNIT- Y: COMPOSITION

1) Readites Comprehension
2) Lender thitinne - Requisition Letcer tor Transiç Cistiticale or Bimatide Certificate ns Attendance Cerlificate



## HAOKS FOR KPFERG.VCO:




## L.EAKNINC OLTCOME:






#  

 B.A.B.ScriB.Com.GENERAL INGLISIA PAPTRR III
(For the students adatited frum the yeur 2019)
HOURS PER WEEK : 4 4
CRFiDITS : $\qquad$
$\qquad$ SHRESTR-III ORIECTHES:



## UNIT-I: POETKY

1) Red. Wed, RedRess Reher: Būn:
2) Poor (iorl - Mayo Ange?


I'Nirt. II: PROSE

1) My Greatest Olymia Prize - Jesse Owens

2) Tuasted Erulish-R K Naragan

## UNIT- III: EXTENSIYE READER

1) Mo:lher's hay - J. B. Priestley
2) Siamond Necklace - Colly De Maupassant

## LINIT- JV; GRAMMAR

1) Vuice- [derlificationt
2) (Tucstiun [ag (with options)
3) Deurecs of Comparison- Identification

## CNir' V : COMPOSITION

I) Readius (:mmprihension
2) Letter writing - Ashing promission to athend cottrection / Permission to go lume.

## BOtM FOR SXCDY:



## BOOKS FOK RFFERE VCE:




## LAARNING OUICOMLE



- E. C"terathers anall l. ite naratives
- Vove di a weli-ntimas Greminar-learning phase
- Auserer tixii wrilinu shols through cumpestion


## 

 GENERAL ENGLISH PAPFK JV (Pre the sturdents admititer firiom the year 2019)HOURS PF.R WEEE ; $\dagger$
CREDTH
: 5
OBdr:CTIvF:K:




## UNIT. I: POETRY

?) A L.inte By's Dean - Katuring Manstick

?) Alt Is Life - Ruskir: Bond

## LiNT' II: PROSE


2) I.ontery Tiaket - Antor Clukoy
3) How To Be A Doctor Steplen [.cacouk

## DNIT- III: FXENSIFE RFADER

1) Refind - firiz Krithy
2) Kiluad - Khushwant Singh

## GNIT- IV: GRAMMAR

1) Yoice - Conversitrn of Siendences
2) Hepported Sputech
ij) Degree af Cothparisoth - Conversiun of Sentences

## UNIT- V: COMPOSITION

1) Job Application with Gover l.cter \& Co
2) Lodering Complaines

## Bnothrade stidyt.



## BOOKS FOR REFEGFNCE:




## L.EARNING OU'TCOME:


 fex!s

- Stengethera their Ge:zrrmar sk:lls
- Are face litaled to write in simple Finglisto meanimetul a their asy to day siluatiens

SKII.1. GASLD ELECTIVL-ENGIASII FOR COMIMLINICATIONI (Fur the studentis admitred from the year 2019) ..... SEMESTLR:I
IOMRS PFR \&VELK : 2
IOMRS PFR \&VELK : 2
CREDIS ..... $: 2$
OBJECTIFFS:
- To matle tle stuler-r


ORAL COMYONEVL
UNIT I
Gectices. Int:oduciry. Secking J'ensissjen
undid
Tedephane Eriquertes
Hand: inuecails - Mocs Ca'ls
[iNIT II]
Reading and Resinconding


## WRITIEN COMPOYENT

## [INIT 1

Giving Insiruetions and Directions
[INIT II
Lewing is Mossaye
Asking for Giving Message
INIT III
Dialoguc Writingịiuided)
© At an interview hall

- At the service cenatc
0 In the Jibrany
o At the bauk
© Naking an unology
I.




## UNIT


 ta.ourlatice a ficstival.;

## BOOKS FOK STLIDY:





## BOOKS FOR RFFERENCE:


2. Developing Commanicativa Skills by Krishto Molan and Meera Banneriec, Macmillan
3. Functionill English by Th. Melathi, Niew C'entury Fook Elouse

## LF.AINING OUTCOMF:

On completion of this tourse the students

- Acyuipe de basics or Speaking and Jesentation skills
* Understand the importionce Non-verbal communcation, gestures and gencral work place sthics
- Develop Writing skills for olificiat puequse
(1..




## LYIT Y





## BOOKS FORSTIDY:





## BOOKSFOR REFERINCE:

1. Form and Junction by $V$. Sasikuanar and $V$. Slyesunala, Jemerald jublishers
2. Duvelaping Communication Skits by Krishiai Wohan and Meera Bamerjec. Atacnilian
?. Functional English by Dr. Malithi. New Centiry Thatk folsiz

## LEARNING OCTCOME:

Or complation of this course the s1udent.

- Acejuire the hasics ol Speakinge arkl Prosemtation skills
- Unders:and the importance Non-Yertal communication. esestures arth general work place ethics
- Develop Writigg skills for official purpose


#  B.A.B.Sc./B.Com. 

## SKII L BASED ELECTIYF - ENGLISH FOR COMMENICATION II

(For the situdents adrnitted from the year 2019:
HOLRS PER WEEK: 2

## CRFAITS


$: 2$

## SFMESTER; II

SUBABCTCODF • 19s\%

## OB.IFCTHE:




## ORAL COMPONENT

['VIT
Smpromptu Talks
UNITT II
Group Disclesiman

## LiNJT [II

Work lutericw \{ FAOsj

## WRITTEN COMAPONENT

[jNITI
Jnteryjews
Maugeing nonverbal cies

## UNIT II

Pablicity Literature - Wititing / Responding 10 Adventsernents

以ハI!

> Role of youlis : molitics
> Morา
> thess bece ic. woltege

> Joddy ": Youtr: inselesp or useti iens"
> Renowine Covers Sports Daly. Aswswation Meeting, Culteral Ceberatior.
> UNTEY

## BOOKS FORSTVDY:



3. Ençish for Competitive Exams by R.E. Bhatnagar

## ROOKS FOR REFERENCE:

1. English and Soliskills by S.l. Dhantavel. Orient [black: wan
2. At of intericuring by H.S Bhatin, Ramesh Publistimug House, New Ochhi
3. Writtco Jinglish for You by Radlakerishua Jidas \& Rajewan, Emerald Publishers

## LFARNING OLITCOME:

On complation of this cuters the sitadents

- comprehend the sigmilicance of dnterviewing and Group Discussion skills
- Develop an incliteation cowurds ageamern :nnd knawitdge of the current topies whith are most debered
- Leam Basic approaches to conmutucation akills and prepare themselves for devis carters


## 

 B.A., B.Sc., B.ConmFNVIROMMINTALSYUDIES



## 

CRFDTS: 2

1 Jシ



- li)


## Lisil 1 : Introduction to F.aviromenent

 In: 1mportace

 Desert tersystem. Ayuitic coosystem:s

## Unit 2 : Vatural Resources: Renewable and Non-renewable Resources


Foresi resousces. Teforestat:un: Causcs anu impacts due to minme. darn buiddine on th Yirunment.
 draughos.
 eneryy sources

## Unil 3 : Biodivmerity and Conservation

Lewels of bisilogical diversity: enentic, specios and easystem divesity; biopengraphy zories al Imdia, butspots
 biodiversity: habitat loss. pouching of wildile, man-uildilic eonfiats. biocosicas invasions. Conscration at biodiversity: ln-situ and $\Gamma$. $x$-situ conserval ion ot liadiversiry.
 Informational value.

## Unit 4 : Finvironmental Pullution

Environmental pullutwon : types, causes, officts ard cantrols: hir. water. stil, ithemical and anse polluiton
Nuclear bazards aud humian frealth risks



 $\because$ vem forsva ian ス!



Trooks Bu Study
 Siladu!ar:ar Source:";


 ?ut|:shine Hisust.

## Boaks for Reference:


 ["ワis. c: Calitumai Press.
 Rourledse.
2. Gicick. ${ }^{2} \mathrm{H}$. : 993. Ware

3. Gixwim. Martha J Gary K. Netee and Cal Ronald carovil. $i^{2}$ rincipica of

 fublishage Co. Pryt T. 1 id .
 Join Wile \& Sons.
 india. Tripahi $]$ gly.
 development. OLIP.
 fiom the Trupic: Jolue wiley \& Surs.
9. wwe sicue.ricie.it


## BHARATHI WOMEN'S COLJEGEVATONOMOUSD, CHFNSAT-GOULOX

## B.A.., B.sc., B.cum <br> value based fiducatyon

(For rter studects adenitterl fremi the vear $3 \boldsymbol{M} 0-30$ ?
Holdes Fet with: 2 (REDHS: 3

## LVIT I








## INTT IT

Fapmily values-dependent - responsitility of the family - neura:ization of ander - idjustability - theats of family :ite . stans of women in famiiy and society - the proclems of day tu day lite faced by Indian monen - -iding fur needy aid elderly - tate :ime alloment for sharing ideas and comezoms.


 - (4


## NNT II)

Ethical values - yrofessit:nal ethics - mass mediu zthice - alvertisement ertus intluence of elhics on a mimily life - psychology of children and youth.

Sucial values - faith, service and secularisinn - saciait scnse and inmmimient sludents and politics.

GIunily CEDíy




## Nivily ${ }^{\circ}$





 !

## BOOK FOR TLDY




.




## BOOK FOH REFERFVCE

## Falue Eutucation

Prof. N,.5. Rightmathan M.s.s., vi imhid.



##  B.S.E.A.B.COM <br> SKIHL DASED BLECTIY! - UI <br> COMPLTING SKJLLS-RASIC (Fat the studeata anmicted from the yelr 2tIt!-20! <br> HOURS PFRWUEEK: A. CREDAS: 2 , <br> $\qquad$ . <br>   <br> $\qquad$

## NMT !




## ENIT II

Processor and membry: Cerotral Pratessing Ureit - connecl unst - Auillmeric and Lowic Lnit (AD ( ) - instrative se: - registers.


## UNII III

Word processing: Cizating a word document - pavirig word document - applying
 ct.ocker, Headers and Fnoters.

## UYit IV

Screadshects: Creating a new excel work onok - suving excel work boek -ilding Jata to cells - insertion and delction oi cells - working with tables aitd chart5 - firmulas and ūmillons.

## References:

 pueblizalinns.
 Necraw Hill.


Horcsermers,
cerime
(By:


 INTi-1: Incudactiou to Personality Deveioponeat:


 2lerennaliry and "festye.

## GNTT-2; Self Auareness and Self Miotitution:





Jiterpermal Relationships - Dcfining the differctice tetween aggessive, submissive and assetive behavieus . Seteral thituking - Tuble Mannere - Table triumettes in Muluculural 5 Evivonnert Dois and Don'ts of Table Etiqiettes - Stress Management - Mcining Sontces ur'siress - Sympturns nt Suces - Consequences of Stress - Managing Stacse.

## EXII. 4: Tinec Management, Leaterstip ajd Decisiun Making:

Plarning \& Goai Setting - Dealing with uther feuple - Anelysis do geals and ocipectives -
Systeraization nt processes - Prioñitzatiann. T.eadership and ẹbattice of a successiui lender cevision raking.

## IXII E.5:Commensication and Graup Discussion:



 requited fer (jronp J) iscussima- Pruccsi of Croup Discussion.

## BOOKXYOHSTUDY:

 Publications, 20!?
2. Stephan P. Robòins, istganisatumal Bè̀avidur. Jctule Ediriun, Prentice Iłall af [adis Prate Litinitad. $\mathrm{V}_{\mathrm{tw}}$ Delidi, 200 K .



